



# **P**assive and **A**ctive **C**ombined **A**ttacks

## **Combining Fault Attacks and Side Channel Analysis**

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# Outline

## ➤ Introduction

- Passive Attack: Power Analysis.
- Active Attack: Fault Attack.
- State of the art.

## ➤ PACA – Combined Attacks

- Principle.
- Application to RSA.

## ➤ Countermeasure

- Detect and Derive.

## ➤ Conclusion / Future Works

# Introduction

- *Two types of countermeasures:*
  - **SCA**: Side Channel Attacks (DPA, SPA, Template-Analysis, Timing Attacks, ...).
  - **FA**: Fault Attacks (Invasive, Transient, ...).
- *Problem:* Each protection is usually focused to protect against **SCA or FA**.
- *Idea:* Combine both kind of attacks to defeat a classical set of countermeasures.
  - **PACA**: Passive and Active Combined Attacks.

## *Introduction: Previous Work*

### ➤ “Optically Enhanced Position-Locked Power Analysis” by Sergei Skorobogatov (CHES’06).

Use a focused laser to enhance the power consumption of a sensitive part in a chip.

- Active Attack : Optical Enhancement of Power Consumption.
- Passive Attack : DPA, ...

### ➤ PACA : A ‘Fashionable’ Attack ?

Presented this morning :

“How can we overcome **both Side Channel Analysis and Fault Attacks** on RSA-CRT ?” by Chong Hee Kim and Jean-Jacques Quisquater.

# ***Passive and Combine Attacks***

**In order to make the attack realistic...**

**...let's take the take the simplest of both worlds.**

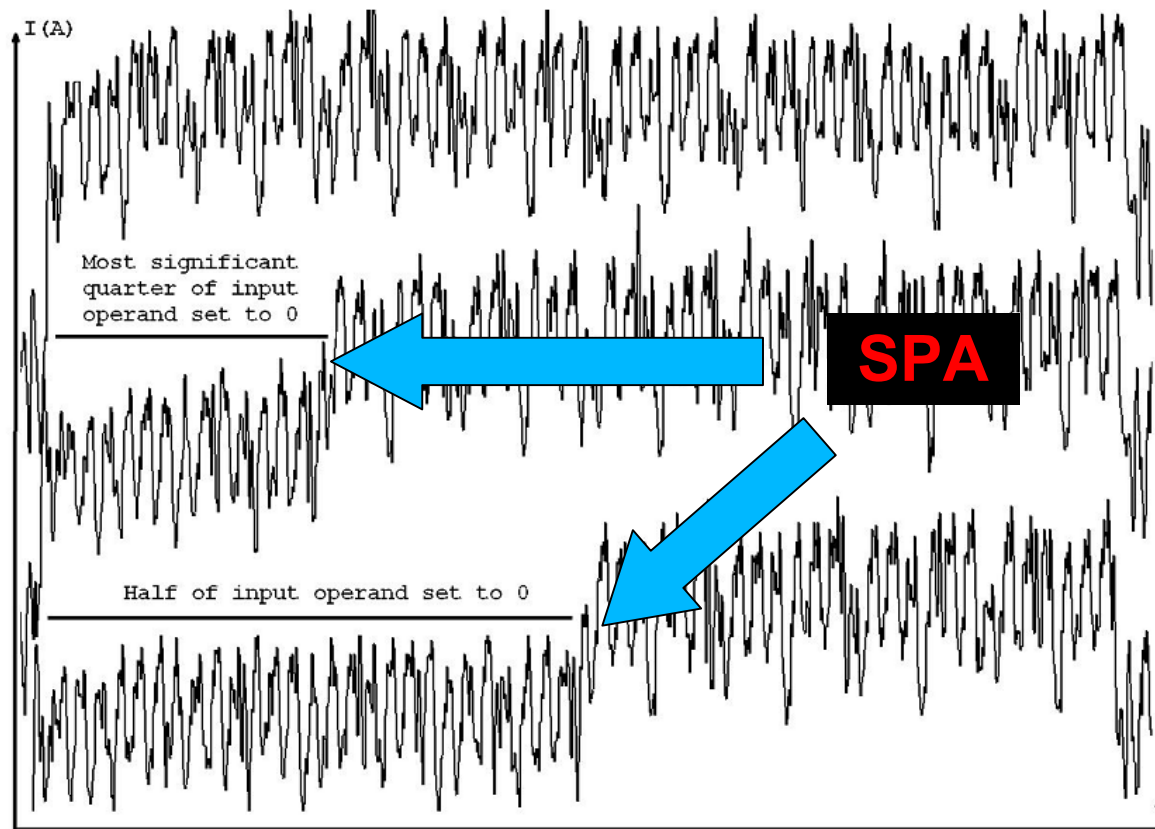
## *Let's choose our Passive Attack...*

- Simplest SCA... Simple Power Analysis !!!
- Particularly adapted to RSA: Need only one curve on naïve implementation to retrieve the private key value.
- Without randomization techniques, well-chosen message can reveal the nature of operation:

**Square or Multiply**

... which give the value of the private key.

# SPA on Multiplication Operation



Square or Mult  
*Random values for Operands*

Mult A x B  
*Quarter of A set to 0*

Mult A x B  
*Half of A set to 0*

# ***Fault Model***

- Modify a part of an input operand.
  - **Corrupt of a word during a memory transfer (typically set to zero).**
  
- Corrupt address pointer of a multiplicand.
  - **Modified pointer value could point to an uninitialized RAM area (also typically set to zero).**
  
- etc.



# Is this RSA implementation protected ?

Compute an RSA signature :  $s = m^d \bmod n$

Countermeasures : **Randomization Scheme** / **Side-Channel Atomicity** / **Fault Protection**

Implementation :

➤ **Get  $r_1, r_2$  two non zero small random values**

➤  **$R_0 = 1 + r_1.n$**

➤  **$R_1 = m + r_1.n \bmod r_2.n$**

➤  **$k = 0$**

➤ **for  $i$  from  $k-1$  to 0 do**

- **$R_0 = R_0.R_k \bmod r_2.n$**
- **$k = k \text{ xor } d_i$**
- **$i = i - \text{not}(k)$**

➤  **$s = R_0 \bmod n$**

➤  **$m_{\text{redundancy}} = s^e \bmod n$**

➤ **if  $m \neq m_{\text{redundancy}}$  then fault detected !**

➤ **else return ( $s$ )**

*It seems...*



## but what would happen if ...

Compute an RSA signature :  $s = m^d \bmod n$

Countermeasures : Randomization Scheme / Side-Channel Atomicity / Fault Protection

Implementation :

✚ Get r1, r2 two non zero small random values

✚  $R0 = 1 + r1 \cdot n$

✚  $k = 0$

✚ for i from k-1 to 0 do

- $R0 = R0 \cdot Rk \bmod r2 \cdot n$
- $k = k \text{ xor } di$
- $i = i - \text{not}(k)$

✚  $s = R0 \bmod n$

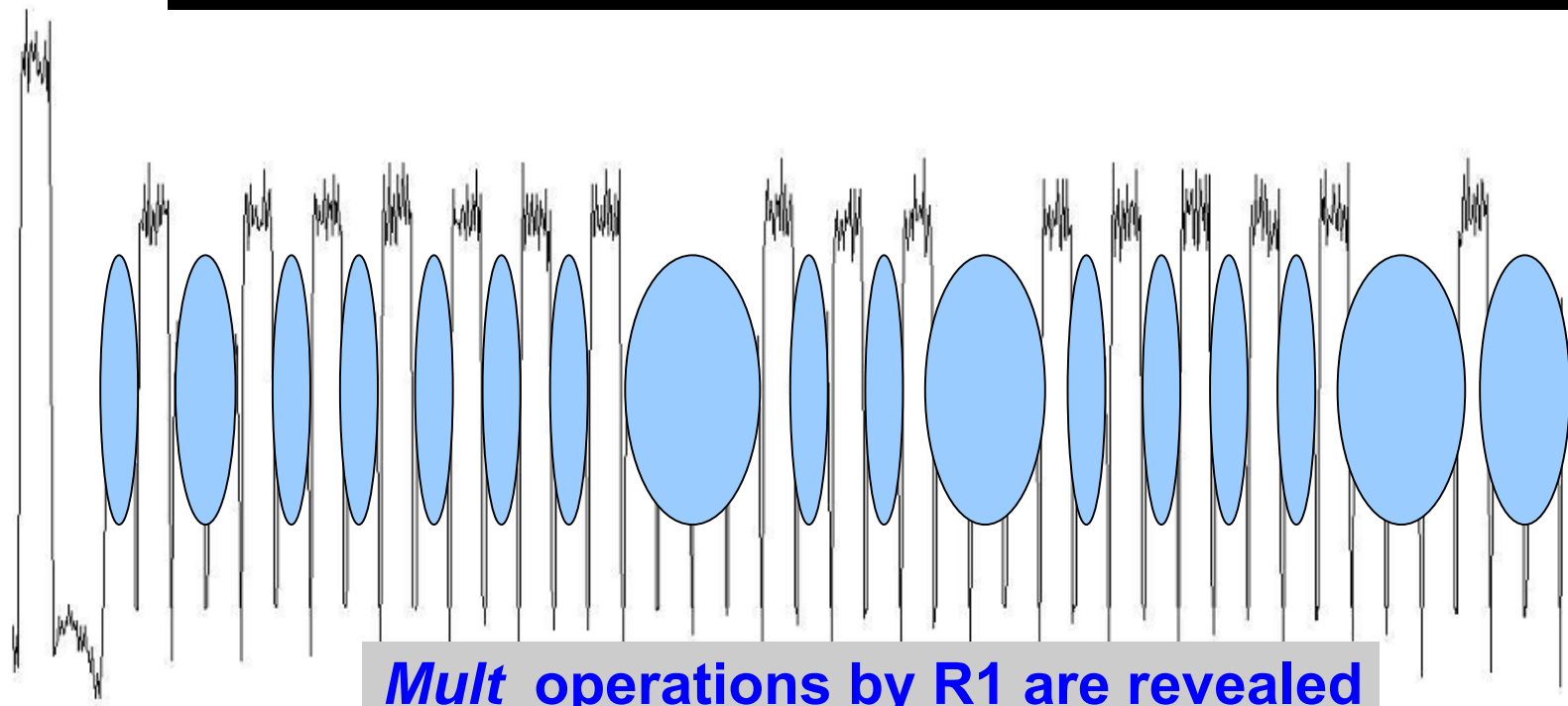
✚  $m_{\text{redundancy}} = s^e \bmod n$

✚ if  $m \neq m_{\text{redundancy}}$  then fault detected !

✚ else return (s)

... this operation is perturbed  
and gives to R1 a low  
Hamming Weight ?

# SPA leakage with only 1 successful fault !



***Mult* operations by R1 are revealed**

# What about the FA countermeasures ?

Compute an RSA signature :  $s = m^d \text{ mod } n$

Countermeasures : Randomization Scheme / Side-Channel Atomicity / Fault Protection

Implementation :

➤ Get r1, r2 two non zero small random values

➤  $R0 = 1 + r1.n$

➤  $R1 = m + r1.n \text{ mod } r2.n$

➤  $k = 0$

➤ for i from k-1 to 0 do

•  $R0 = R0.Rk \text{ mod } r2.n$

•  $k = k \text{ xor } di$

•  $i = i - \text{not}(k)$

➤  $s = R0 \text{ mod } n$

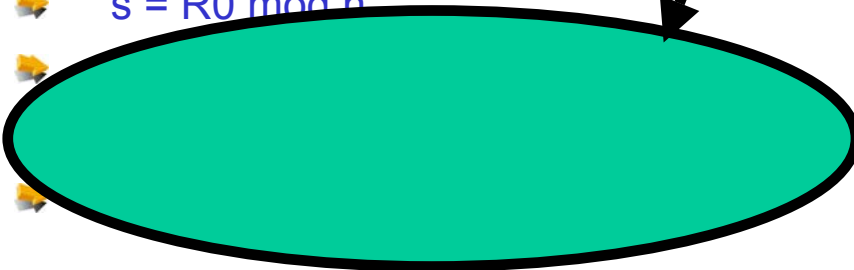
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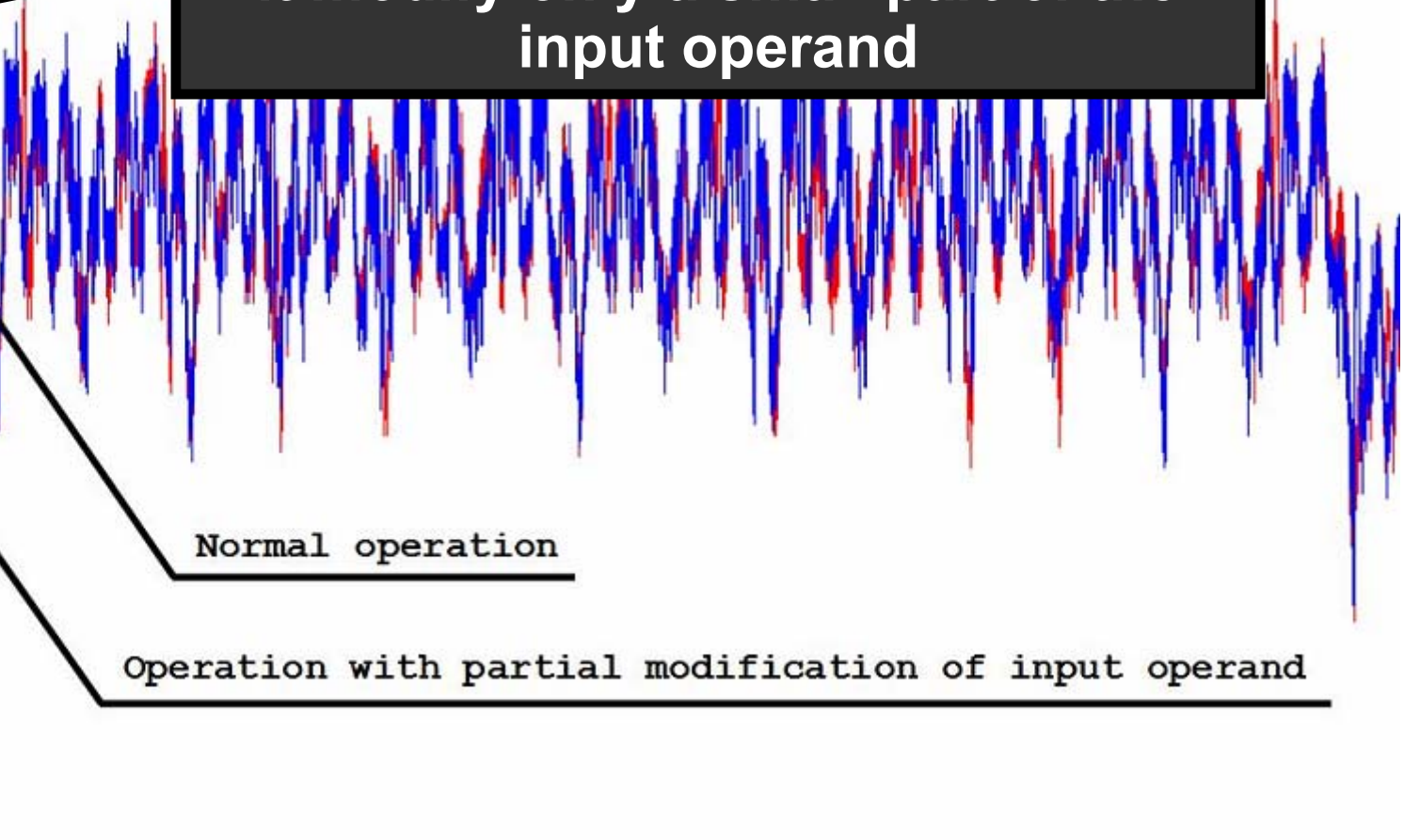
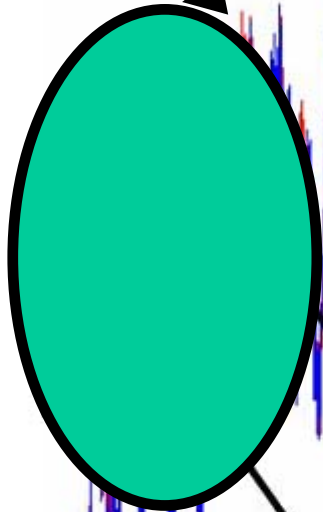
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Problem : The fault will be detected but too late, the side channel leakage can be exploited !



# Side Channel Leakage

The fault could be exploited even if it modify only a small part of the input operand



Normal operation

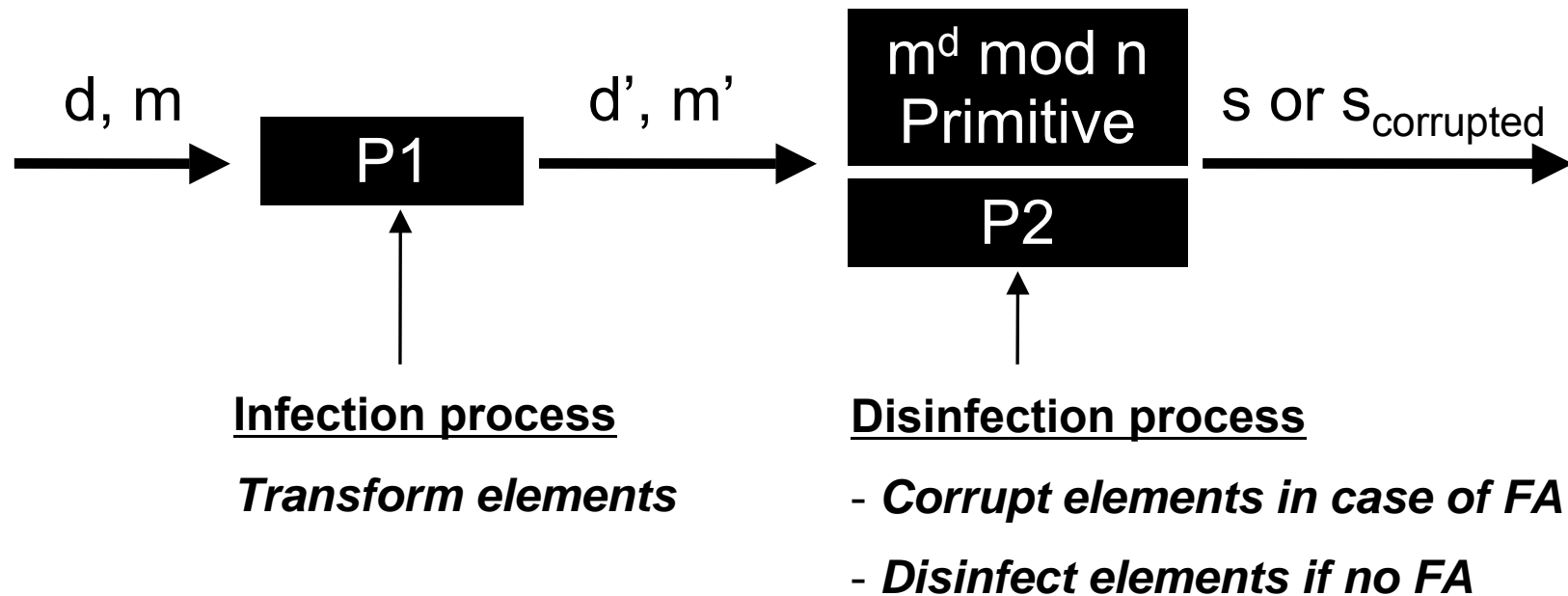
Operation with partial modification of input operand

# ***Possible Countermeasures***

- **Detect And Derive !**
- **Corrupt secret data in an non-invertible way before the sensitive process if a fault is detected.**
- **During the sensitive process execution, data is untransformed if no fault is detected.**

# Detect And Derive !

➤ Example on RSA Signature -  $s = m^d \text{ mod } n$





# Detect And Derive ! -- RSA Implementation 1

- let  $d_{\text{check}} = \Psi(n, d, m)$ 
  - typically  $d_{\text{check}}$  would be checksum..
  
- let  $U = d_{\text{check}} \mid d_{\text{check}} \mid \dots \mid d_{\text{check}}$
  
- $d^* = d \text{ XOR } U$
  
- during the exponentiation loop:
  - for each word  $d_i^*$  of  $d^*$  :
    - compute  $d_{\text{check}} = \Psi(n, d, m)$
    - $d_i = d_i^* \text{ XOR } d_{\text{check}}$
  
- So the corruption of  $d$ ,  $n$  or  $m$  will imply the computation of a signature with a wrong *private key* value !

## ***Detect And Derive ! -- RSA Implementation 2***

- $d = (d_{k-1}, \dots, d_1, d_0)$  the RSA private key.
- let ID be a secret number.
- let  $A = \Psi(n, d, m)$
- let  $f$  be a bitwise function.
- compute  $d^*$  such as :
  - $d_{k-1}^* = d_{k-1} \text{ XOR } f(\text{ID}, A)$
  - For  $i$  from  $k-2$  to  $0$ 
    - $d_i^* = d_i \text{ XOR } f(d_{i+1}^*, d_{i+1})$
- before the exponentiation loop :
  - $B = \Psi(n, d, m)$
- during the exponentiation :
  - Compute for each loop :  $d_i = d_i^* \text{ XOR } f(d_{i+1}^*, d_{i+1})$
- So the corruption of  $d$ ,  $n$  or  $m$  element will sequentially corrupt the whole  $d_i$  sequence.

# Conclusion

- **New class of combined attacks.**
  - Experiments were conducted on “protected” implementation.
  - Only 1 successful fault is necessary to recover the entire private exponent value on certain implementations.
  
- **Need careful design of cryptographic modules.**
  - Important literature on fault or side channel protections but may not be enough to protect against PACA.
  - *Detect And Derive* strategy presented.
  
- **Not limited to RSA ...**



***Questions ?***