

MAYo or MAY-not: Exploring Implementation  
Security of the Post-Quantum Signature Scheme MAYO Against Physical Attacks

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# Attacking MAYO with loop-abort/Zeroing faults

1

MAYO is post-quantum secure multivariate signature scheme notable for its efficient and compact key size

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This paper: Studying the resilience of MAYO against fault injection attacks

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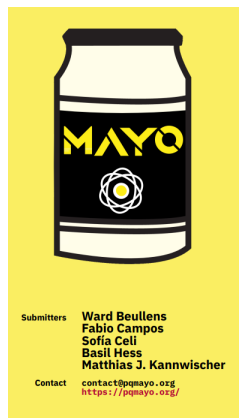
We present loop-abort fault attacks on MAYO, which allow for full key recovery with only one fault

# Motivation: MAYO is promising multi-variate digital signature candidate, but only limited research on Mayo's resilience against physical attacks



## Call for Additional Digital Signature Schemes for the Post-Quantum Cryptography Standardization Process

*Updated October 2022 to reflect that IP statements can be accepted digitally.*



- MAYO, a multi-variate signature scheme was submitted, to the NIST call for additional post-quantum secure digital signature schemes
- MAYO features compact key and signature size and is notable for its efficiency
- MAYO has so far withstood cryptanalysis
- But: Only limited research on MAYO's implementation security against physical attack exists



**Research Question:** What is MAYO's attack surface against fault injection attacks?

## Recap: Multivariate Signature Schemes -- Signing

- Multivariate cryptographic schemes base their security on the hardness of solving a set of multivariate quadratic equations over a small finite field  $F$  --- One instantiation: **Unbalanced oil and vinegar schemes**
- **Public Key:** Trapdoored homogenous multivariate map:

$$P(x) = (p_1(x), \dots, p_m(x)): \mathbb{F}_q^n \rightarrow \mathbb{F}_q^m$$

where  $p_1(x), \dots, p_m(x)$  are multivariate quadratic polynomials in  $n$  variables  $x=(x_1, \dots, x_n)$

- **Trapdoor/Private Key:** Secret subspace  $O \subseteq \mathbb{F}_q^n$  (oil space) of dimension  $m$  on which  $P(x)$  evaluates to zero
- **Signing:** Hash message to target vector  $t \in \mathbb{F}_q^m$  and find preimage under map  $P$  -- Doing so without the trapdoor is hard.

## Recap: Multivariate Signature Schemes -- Signing

- Signing a message: Find a preimage  $s$  to target vector  $t$  under map  $P$
- **Observation:** This is easy to do given access to the oil space!
  - Define the polar form or differential of map  $P$  of a multi-variate quadratic polynomial as:

$$P'(x, y) = P(x + y) - P(x) - P(y)$$

- To find a pre-image of a target vector  $t$ , having knowledge of the oil space  $O$ :
  1. first pick a random vinegar vector  $v$  and
  2. then solve  $P(v + o) = t$  for a vector  $o \in O$  by solving the linear equation system:

$$\underbrace{P'(v, o)}_{\text{Linear in } o} + \underbrace{P(o)}_{= 0} + \underbrace{P(v)}_{\text{fixed}} = t$$

## Recap: MAYO

- **Drawback of UOV schemes:** UOV schemes have a small signature size, secure parameter sets lead to key pairs of enormous size (e.g., 50 KB)
- **Key Idea Of Mayo: Stretch the public key map  $P$  into a larger map**, such that it accepts  $k$  input vectors  $x_i \in \mathbb{F}_q^n$

$$\mathcal{P}^*(\mathbf{x}_1, \dots, \mathbf{x}_k) := \sum_{i=1}^k \mathbf{E}_{ii} \mathcal{P}(\mathbf{x}_i) + \sum_{1 \leq i < j \leq k} \mathbf{E}_{ij} (\mathcal{P}'(\mathbf{x}_i, \mathbf{x}_j)),$$

where  $E_i$  are fixed, public,  $m$ -by- $m$  matrices


- **This allows for small parameters and public key and signature sizes.** For example, in Mayo NIST-Security Level 1 (=as hard as breaking AES-128):
  - **Params:**  $\dim(O) = 8, m = 64, n = 66, q = 16, k = 9$ , **Public Key:** 1168 Bytes, **Signature** 321 Bytes

## Recap: MAYO Signature Algorithm

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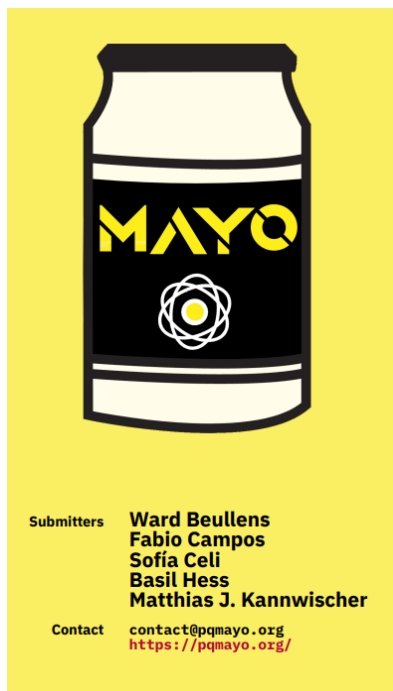
### Algorithm 2 Sign( $M, sk$ )

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- 1: (seed,  $\mathbf{O}$ )  $\leftarrow$  sk
  - 2: salt  $\leftarrow \{0, 1\}^{2\lambda}$
  - 3:  $t \leftarrow \text{Hash}(M \parallel \text{salt})$
  - 4:  $\mathcal{P}^*(\mathbf{x}_1, \dots, \mathbf{x}_k) \leftarrow \sum_{i=1}^k E_{ii} \mathcal{P}(\mathbf{x}_i) + \sum_{1 \leq i < j \leq k} E_{ij} \mathcal{P}'(\mathbf{x}_i, \mathbf{x}_j)$
  - 5:  $\mathbf{v}_i \leftarrow \mathbb{F}_q^{n-m} \times \{0\}^m$  
  - 6: **if**  $\mathcal{P}^*(\mathbf{v}_1 + \mathbf{o}_1, \dots, \mathbf{v}_k + \mathbf{o}_k)$  does not have full rank **then**
  - 7:     return to step 5
  - 8: **end if**
  - 9: Solve  $\mathbf{P}^*(\mathbf{v}_1 + \mathbf{o}_1, \dots, \mathbf{v}_k + \mathbf{o}_k) = \mathbf{t}$  for  $\mathbf{o}_1, \dots, \mathbf{o}_k \in \text{RowSpace}(\mathbf{O} \parallel \mathbf{I}_o)$ .
  - 10: **return**  $\sigma = (\text{salt}, \{\mathbf{s}_i = \mathbf{v}_i + \mathbf{o}_i\}_{i \in [k]})$
-



# MAYO is a promising candidate, but research on resilience against physical attacks is missing



- Given its compactness and efficiency MAYO is a promising PQC Signature candidate
- More compact than ML-DSA (standardized Dilithium) and Falcon (selected for standardization)
- We can expect deployment on embedded systems, which need to be secure against physical attacks



**Research Question:** What is MAYO's attack surface against fault injection attacks?

## This Paper: Loop-abort attacks against Mayo



We present two, first-order fault-injection attack scenarios against MAYO that allow full key recovery

# Fault Injection attacks against Mayo



Faulting the sampling of one out of the  $k$  vinegar vectors reveals information about the corresponding oil vector --- which can allow for secret key recovery.

- Key Idea: Prior work has shown that **if an attacker knows one oil vector, recovering the entire oil space is merely a matter of solving linear equations** (with techniques borrowed from the reconciliation attack, see [Beu21b])
- Thus: If we can disturb the sampling of a vinegar vector, this reveals information about the corresponding oil vector, allowing us to recover the secret key!
  - Prior work has successfully attacked Rainbow by faulting the sampling of the vinegar vectors (and fault attacks on Rainbow [AKKM22]) – we combine this attack with the reconciliation attack to only use one fault)



We present two, first-order fault-injection attack scenarios against MAYO that allow full key recovery

We will establish the result in two steps:

1. **Given access to an oil vector, how can we recover the entire oil space?**
2. How can we can reveal an oil vector from a faulted signature?

## Reconciliation attack for MAYO

Assume we recovered an oil vector  $o_1 \in O$  and want to recover an additional oil vector  $o_2 \in O$ . We need to solve the system:

$$\begin{aligned}P(o_2) &= 0 \\P'(o_1, o_2) &= 0\end{aligned}$$

- For a given  $o_1$  the differential map  $P'(o_1, o_2) = 0$  imposes  $m$  linear equations in the entries of  $o_2$  (each polynomial in  $P'(o_1, o_2)$  provides a  $P'$ linear equation in  $n$  variables)
- Since  $o_2 \in \mathbb{F}_q^n$  this system is under-constrained.
- But:  $\dim(O) > n - m$ , that is, we can fix  $n - m$  entries of  $o_2$  and solve linear system
- Full key recovery in  $O(o \cdot m^3)$  (for all security levels,  $o, m, n < 150$ )



We present two, first-order fault-injection attack scenarios against MAYO that allow full key recovery

We will establish the result in two steps:

1. Given access to an oil vector, how can we recover the entire oil space?
2. **How can we can reveal an oil vector from a faulted signature?**

## Recap: MAYO Signature Algorithm

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### Algorithm 2 Sign( $M, sk$ )

---

- 1:  $(seed, \mathbf{O}) \leftarrow sk$
  - 2:  $salt \leftarrow \{0, 1\}^{2\lambda}$
  - 3:  $t \leftarrow \text{Hash}(M || salt)$
  - 4:  $\mathcal{P}^*(\mathbf{x}_1, \dots, \mathbf{x}_k) \leftarrow \sum_{i=1}^k E_{ii} \mathcal{P}(\mathbf{x}_i) + \sum_{1 \leq i < j \leq k} E_{ij} \mathcal{P}'(\mathbf{x}_i, \mathbf{x}_j)$
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- 

for  $i=1$  to  $k$ :

$\mathbf{v}[i] = \text{decode}(\text{shake256}(\text{randomness}))$



Vinegar vectors are sampled in nested loop in sequential order – we can fault to abort the loop, skipping the sampling of a vector!

## Loop-abort attacks against Mayo (Scenario 1)



Scenario 1: Assume vinegar vectors are initialized to constant, known, value before being sampled.



Assume induced fault skips sampling of a vinegar vector: Resulting signature immediately reveals corresponding oil vector.

```
for i=1 to k: //Fault here
```

```
v[i] = decode(shake256(randomness))
```

Assume we fault the sampling of vector  $v_k$  and all vectors are initialized to zero before: Then resulting signature  $s$  after faulting the sampling of  $v_k$  is :

$$s = (s_1, \dots, s_k) = (v_1 + o_1, \dots, v_k + o_k) = (v_1 + o_1, \dots, \mathbf{0} + o_k)$$

Immediately revealing vector  $o_k$ !



## Loop-abort attacks against Mayo (Scenario 2)



Scenario 2: Differential Fault Attack: Attack first lets the device compute a signature  $s$  correctly, then inject a loop-abort fault during the computation of a second signature  $s'$ .

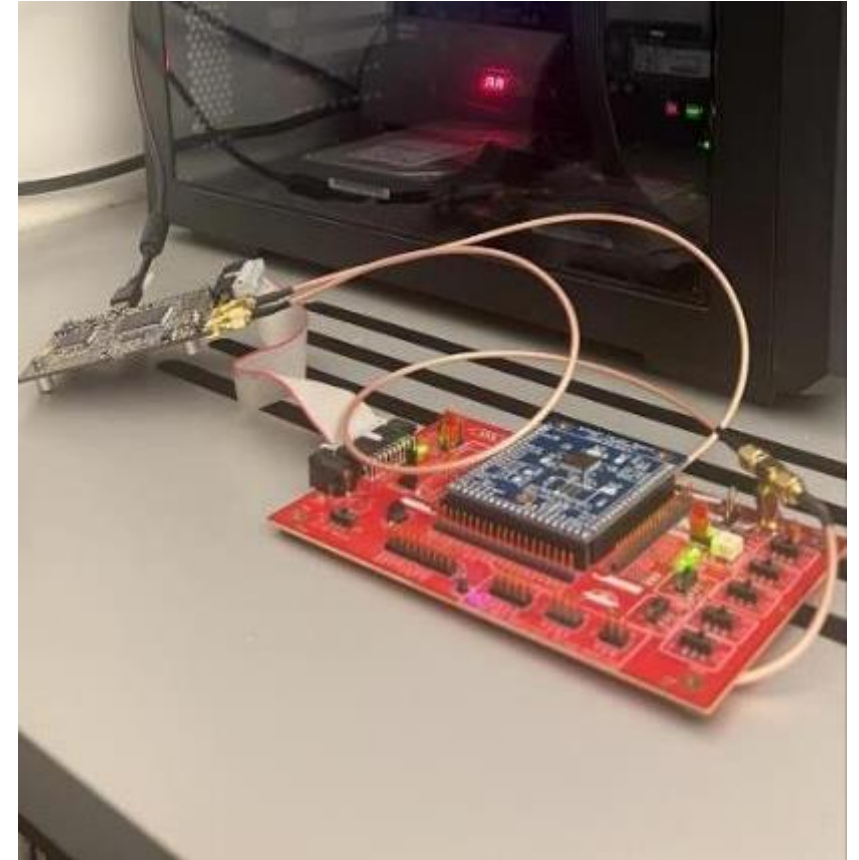


If this fault leads to repetition of vinegar values, then can compute an oil vector from the two signatures

- Assume loop-abort fault results in at least one vinegar vectors  $v_i'$  being assigned the same value as in the first (correct) signature
- Then: can recover oil vector  $v_i$  given a pair of faulted and non-faulted signature  $(s_i', s_i)$  through  $s_i - s_i' = v_i + o_i - v_i' - o_i' = o_i - o_i'$  which is again a vector the oil space!
- Does not require the other (non-faulted) vinegar values to be the same in both signatures – works against even the randomized version of MAYO!
- Example real-world scenario: Vinegar values are allocated in memory, but not initialized. Skipping the vinegar sampling could result in re-using the values that were in memory before.

## Theoretical and Practical Evaluations succeeded

- **Theoretical Evaluation:** Simulated faults in the SAGE implementation of Mayo as submitted to the NIST competition: Key recovery in less than a minute for both scenarios!
- **Practical Evaluation:** Implemented a clock-glitching attack using the ChipWhisperer, executing Mayo's original C implementation on an STM32F4 target board.
  - Successfully skipped the vinegar sampling loop using a clock-glitch, resulting in an oil-vector revealing signature!



# Conclusion

1

By faulting the sampling of the vinegar values, attackers can reveal an oil vector with only one fault.

2

One oil vector is sufficient to recover the entire oil space in minutes

3

This attack results in valid signatures and can attack the non-deterministic version of MAYO, and therefore need additional countermeasures to defend against